

Bounds on unparticle interactions with the electroweak sector

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Simon Knapen, Rutgers University

Hidden CFT sectors (unparticles)

Motivation

- Calculability
- New signatures
- bonus: some model independence

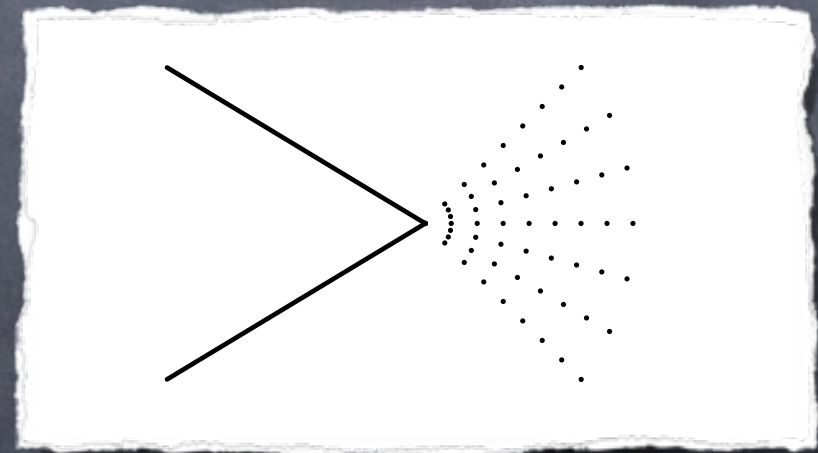
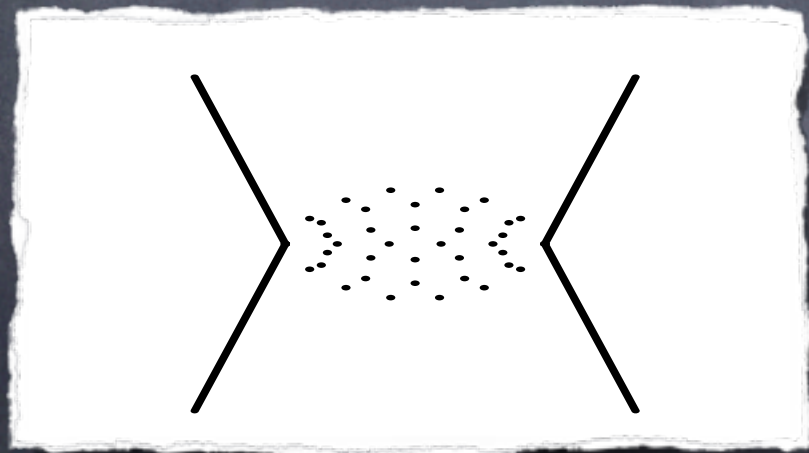
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Hidden CFT sectors (unparticles)

Motivation

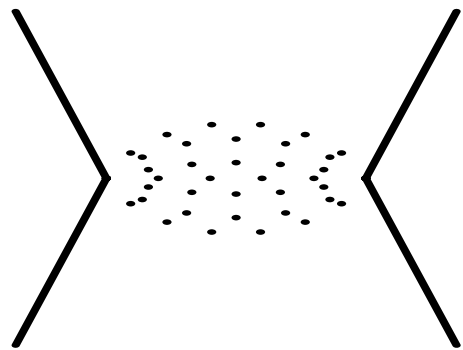
- Calculability
- New signatures
- bonus: some model independence

Signatures

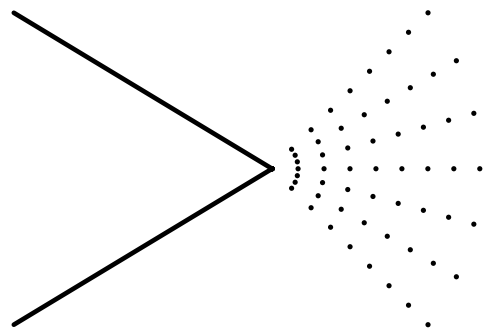


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Calculability



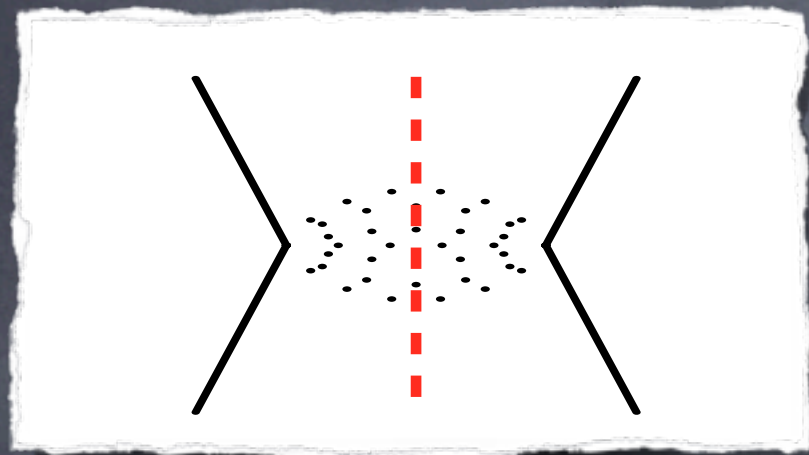
$$\frac{C}{(x_1 - x_2)^{2\Delta}} \rightarrow iA_{\Delta}\theta(p_0)\theta(p^2)(p^2 + i\epsilon)^{\Delta-2}$$



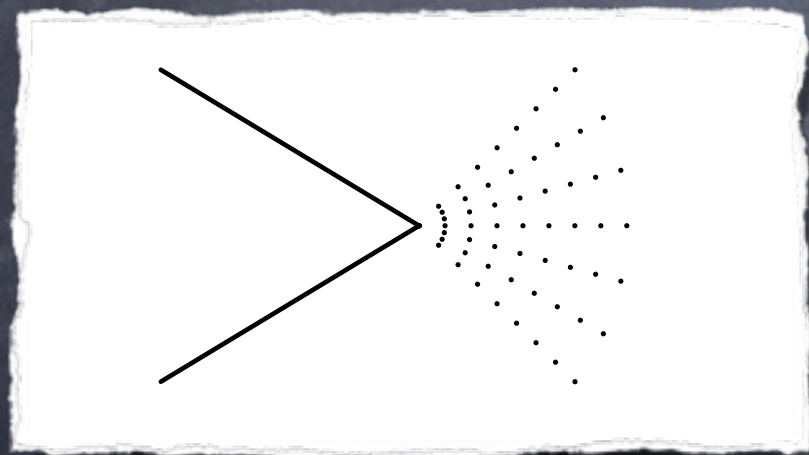
H. Georgi (2007)

Simon Knapen, Rutgers University

Calculability



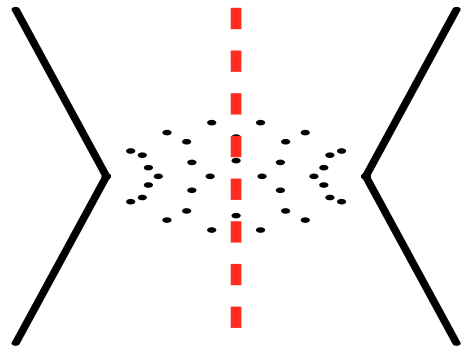
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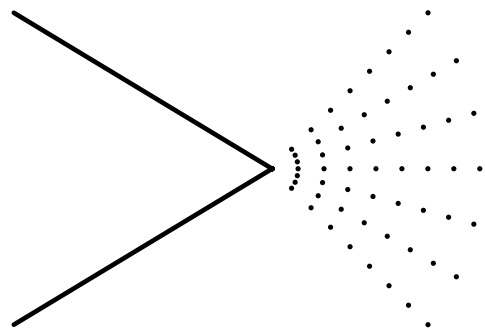
H. Georgi (2007)

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Calculability



$$\frac{C}{(x_1 - x_2)^{2\Delta}} \rightarrow iA_{\Delta}\theta(p_0)\theta(p^2)(p^2 + i\epsilon)^{\Delta-2}$$



1. Compute σ (n massless particles)
2. Analytic continuation $n \rightarrow \Delta$

H. Georgi (2007)

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Coupling with SM

$$\frac{1}{\Lambda^\Delta} F_{\mu\nu} F^{\mu\nu} \mathcal{O}_u$$



$$\left. \begin{aligned} \partial A \partial A \mathcal{O}_u \\ \partial A \partial Z \mathcal{O}_u \\ \partial G \partial G \mathcal{O}_u \end{aligned} \right\}$$

S. Kathrein, SK, M. Strassler
(2010)

A. Delgado, M. Strassler
(2010)

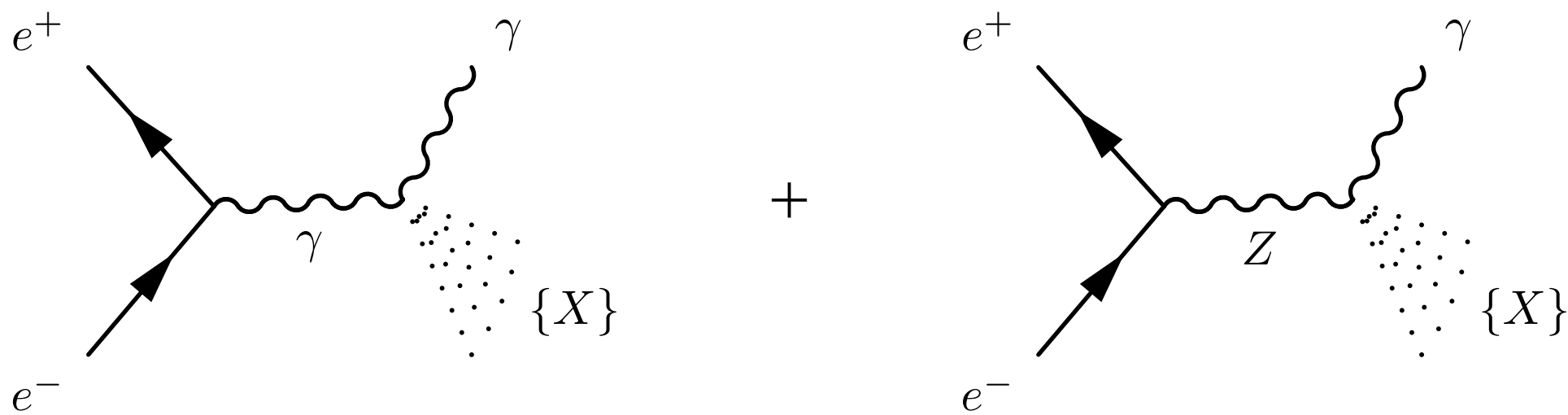
$$1 < \Delta < 2$$



dimension 5 or higher

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Diagrams



$$\frac{d^2\sigma}{dq d\cos\theta} = \frac{(4\pi)^{1-2\Delta}}{\Gamma(\Delta-1)\Gamma(\Delta)} A(\Lambda_{\gamma Z}, \Lambda_{\gamma}) e^2 q^3 s^{\Delta-3} \left(1 - 2\frac{q}{\sqrt{s}}\right)^{\Delta-2} (1 + \cos^2\theta)$$

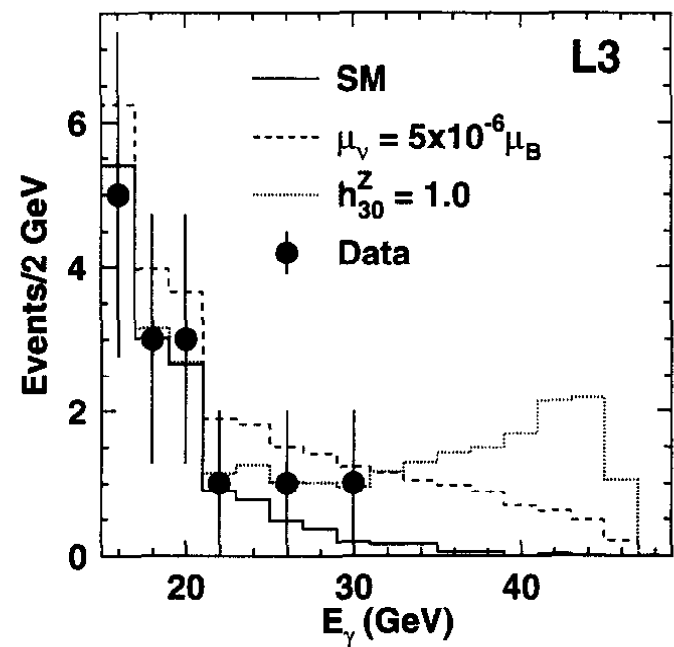
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LEP I & II

(ALEPH, OPAL, DELPHI & L3)

LEP I ($\sqrt{s} = 90$ GeV)

LEP II ($\sqrt{s} = 190\text{--}210$ GeV)



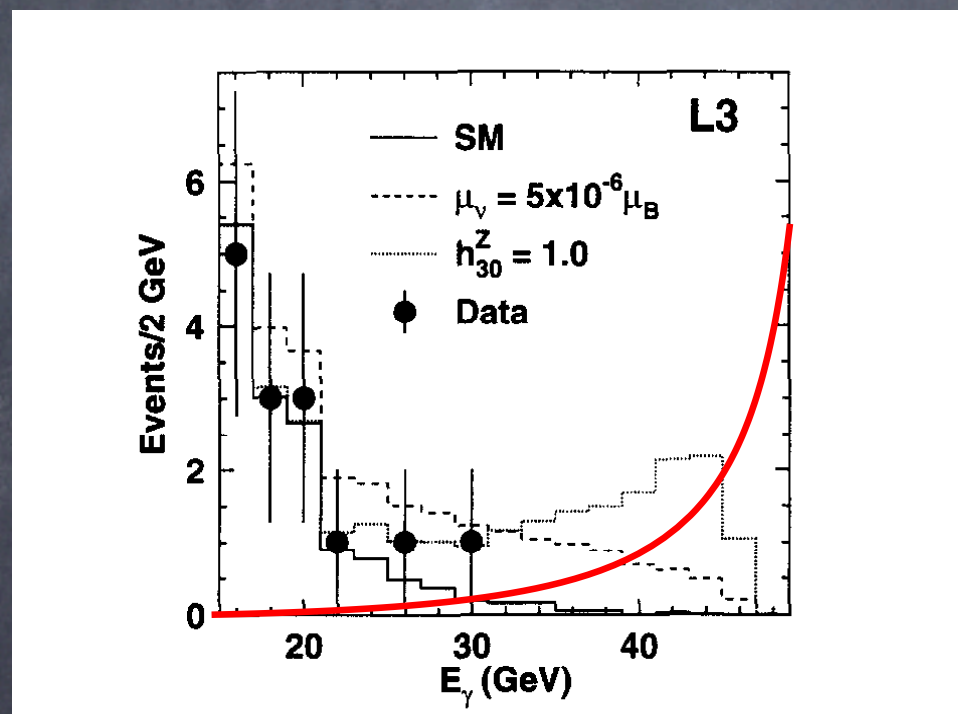
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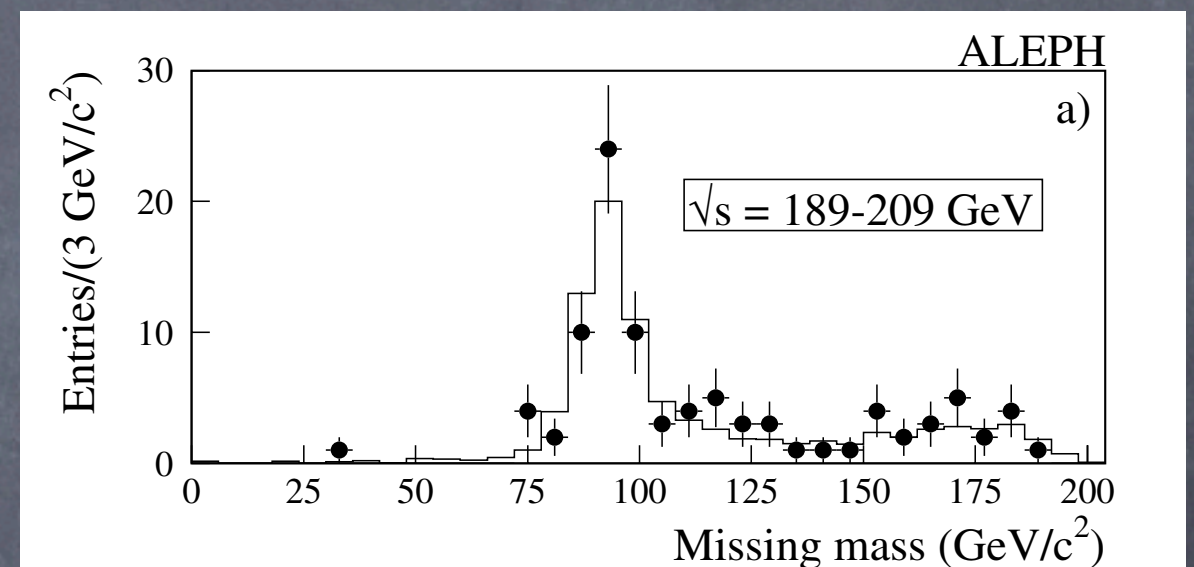
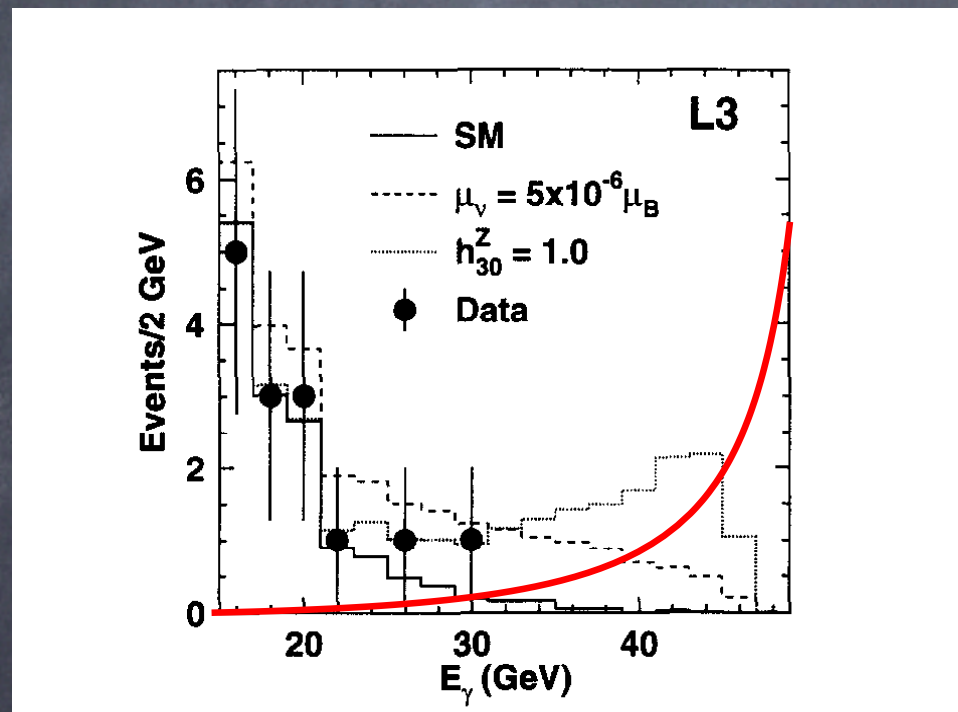
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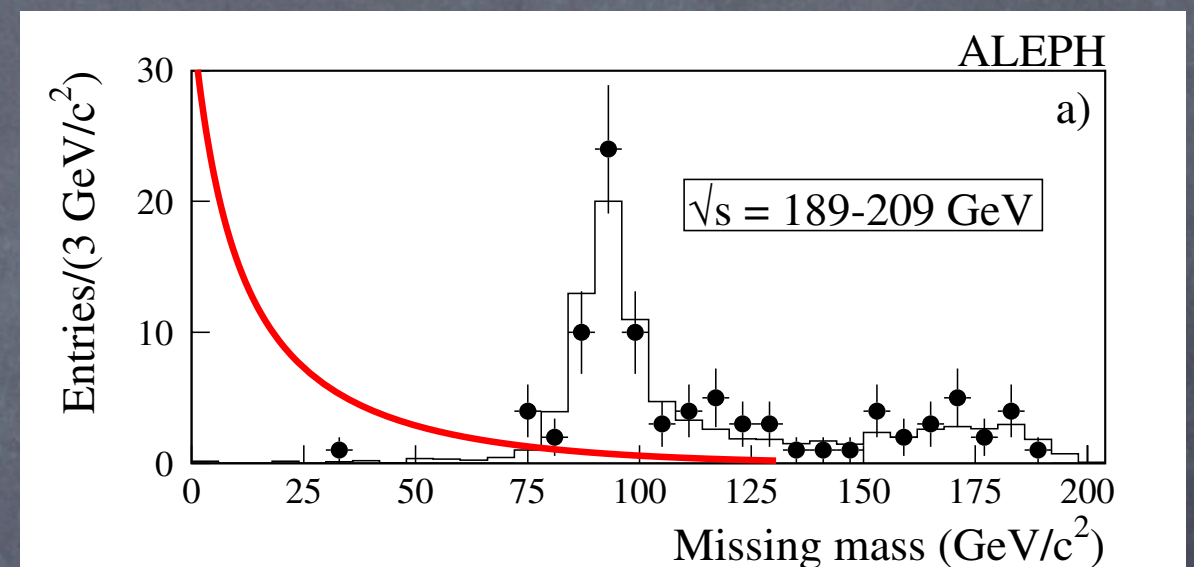
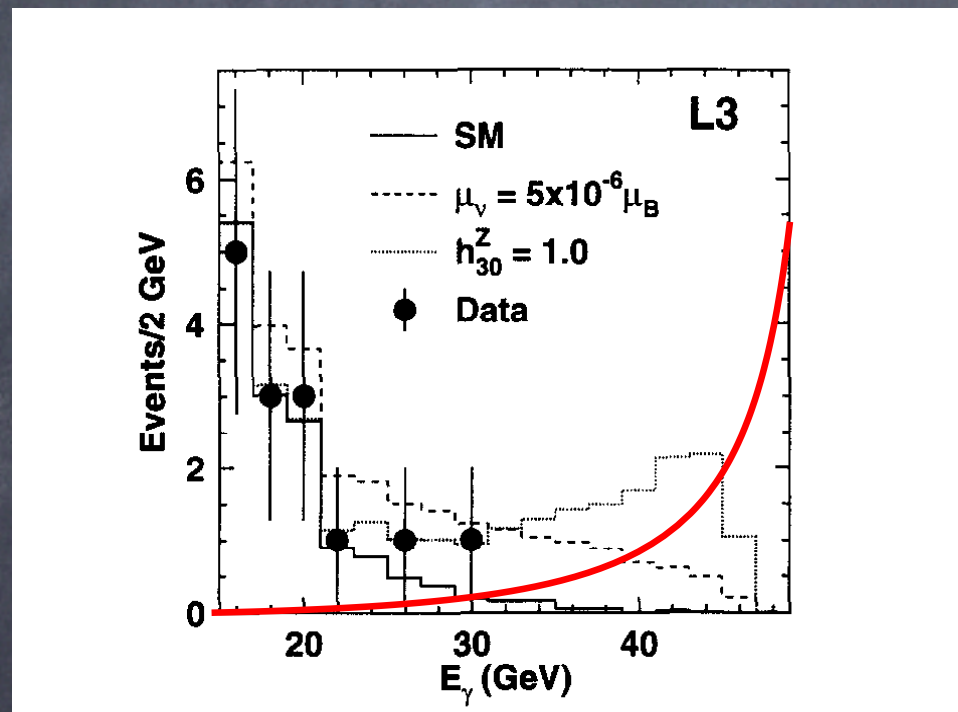
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LEP I & II

(ALEPH, OPAL, DELPHI & L3)

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LEP II ($\sqrt{s} = 190-210$ GeV)



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Experimental Bounds

95% CL (TeV)

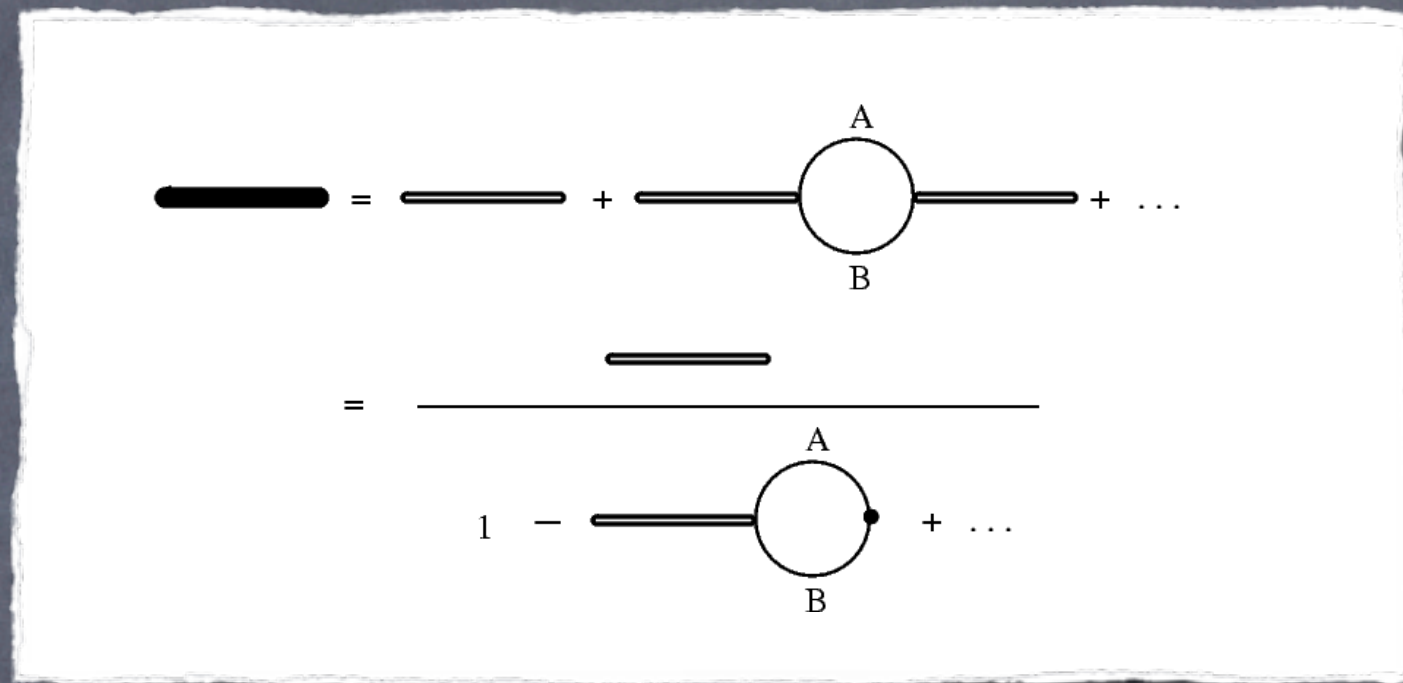
Δ	Λ_Z	Λ_γ
1	69.5	25.2
1.01	59.0	23.0
1.05	40.7	13.2
1.1	26.6	8.0
1.2	12.7	3.6
1.3	6.8	2.0
1.4	4.0	1.2
1.5	2.5	0.79
1.6	1.6	0.57
1.7	1.1	0.41
1.8	0.80	0.30
1.9	0.60	0.24
2	0.46	0.19

$$\frac{1}{\Lambda_Z} \partial A \partial Z \mathcal{O}_u$$

$$\frac{1}{\Lambda_\gamma} \partial A \partial A \mathcal{O}_u$$

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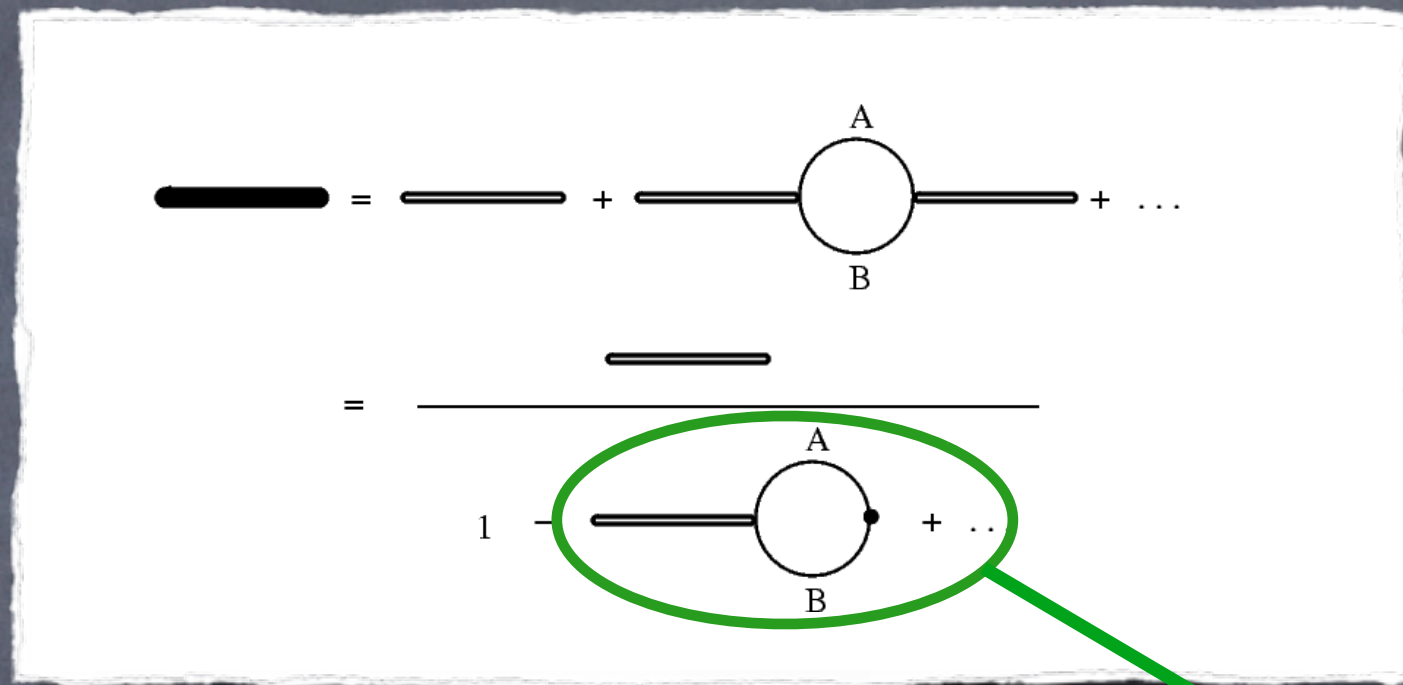
Theory Bounds



A. Delgado, M. Strassler
(2009)

Simon Knapen, Rutgers University

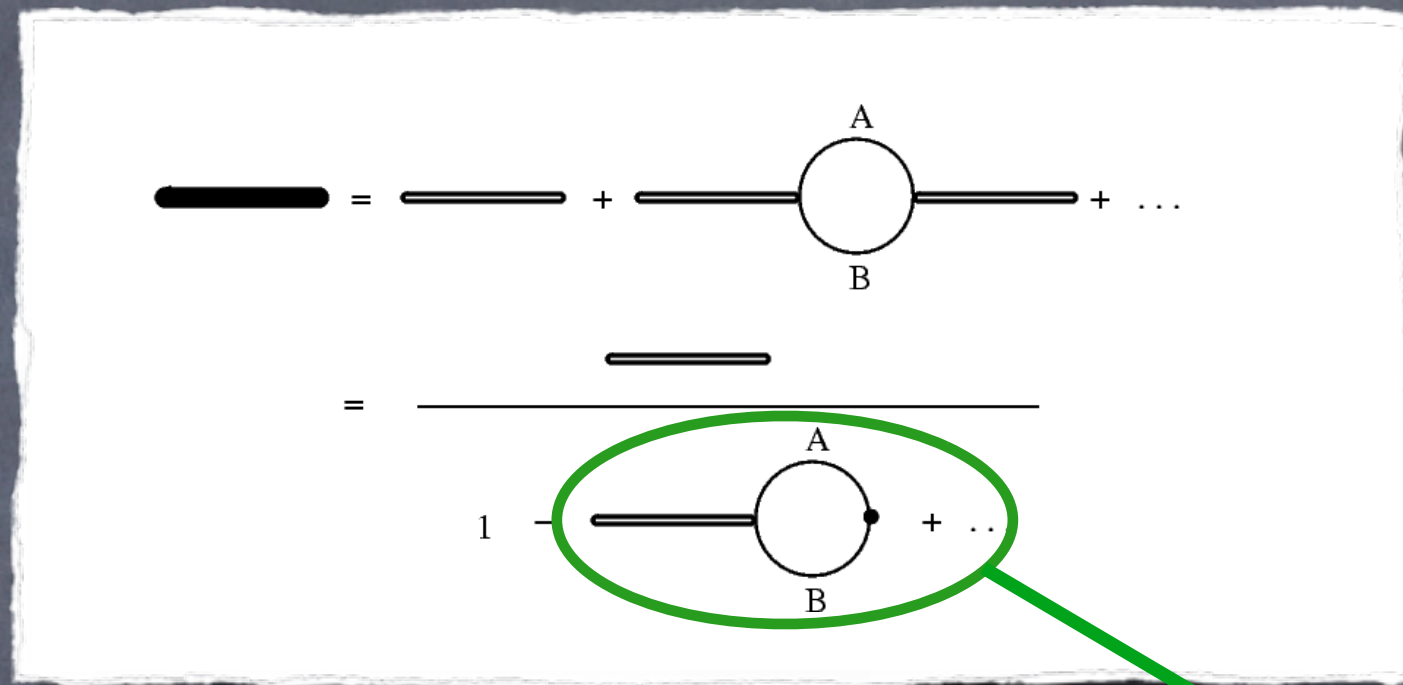
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Theory Bounds



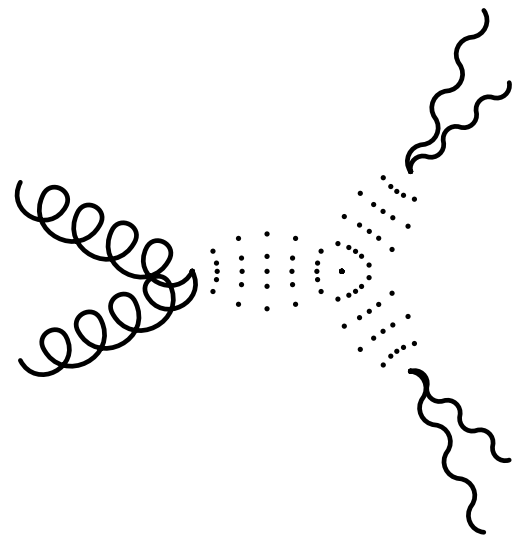
Grows with \hat{S}

Conformal invariance must break down in
the UV

A. Delgado, M. Strassler
(2009)

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Application: $gg \rightarrow 4\gamma$



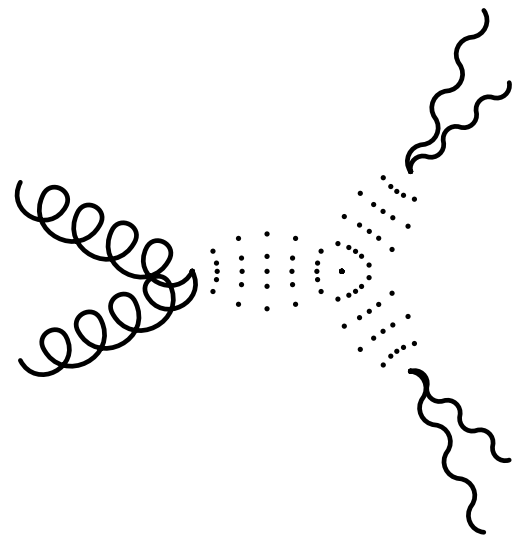
$$\sim \left(\frac{C_3}{\Lambda_g^{\Delta_g} \Lambda_\gamma^{2\Delta_\gamma}} \right)^2$$

$$\sim \langle \mathcal{O}_g \mathcal{O}_\gamma \mathcal{O}_\gamma \rangle$$

J. L. Feng, A. Rajaraman and H. Tu (2008)

Simon Knapen, Rutgers University

Application: $gg \rightarrow 4\gamma$



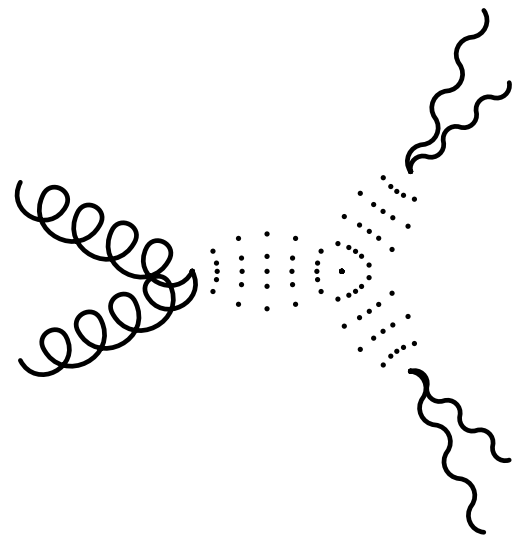
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$$\sim \left(\frac{C_3}{\Lambda_g^{\Delta_g} \Lambda_\gamma^{2\Delta_\gamma}} \right)^2$$

$$\sim \langle \mathcal{O}_g \mathcal{O}_\gamma \mathcal{O}_\gamma \rangle$$

J. L. Feng, A. Rajaraman and H. Tu (2008)

Bound individually:

$\Lambda_g \rightarrow$ Tevatron (A. Delgado, M. Strassler (2009))

$\Lambda_\gamma \rightarrow$ LEP (S. Kathrein, SK, M. Strassler (2010))

$C_3 \rightarrow$ Unitarity, Conformal symmetry (F. Caracciolo and S. Rychkov (2010))

Only for $1 < \Delta_\gamma < 1.7$

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Unitarity bound

$$1 < \Delta_g < 2$$

$$1.7 < \Delta_\gamma < 2$$



No bound on C_3 available

A. Delgado, M. Strassler
(2009)

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Unitarity bound

$$\begin{array}{l} 1 < \Delta_g < 2 \\ 1.7 < \Delta_\gamma < 2 \end{array} \longrightarrow \text{No bound on } C_3 \text{ available}$$

No process that involves the hidden sector can have a rate that exceeds the rate of all such processes

A. Delgado, M. Strassler
(2009)

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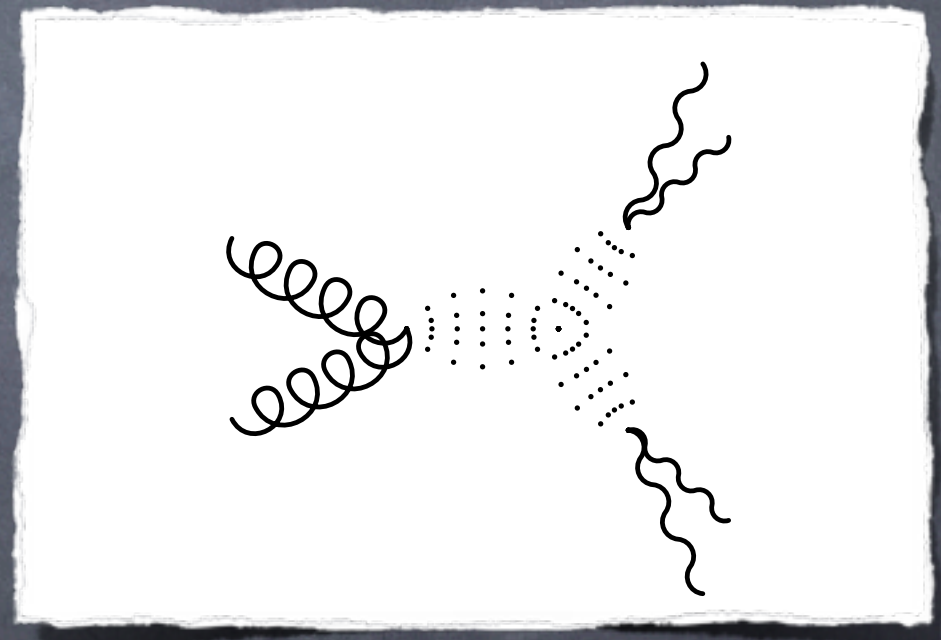
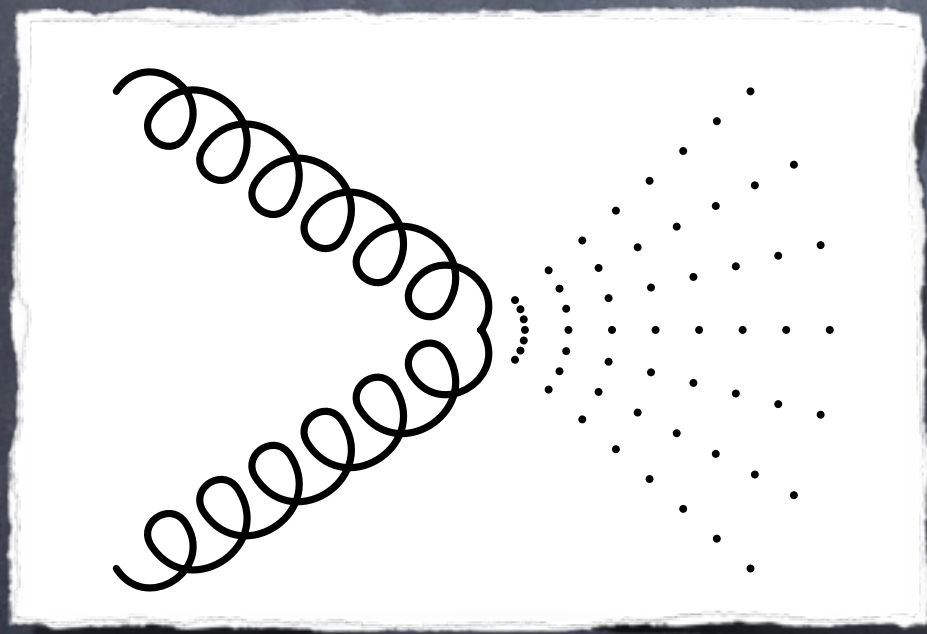
Unitarity bound

$$1 < \Delta_g < 2$$

$$1.7 < \Delta_\gamma < 2$$



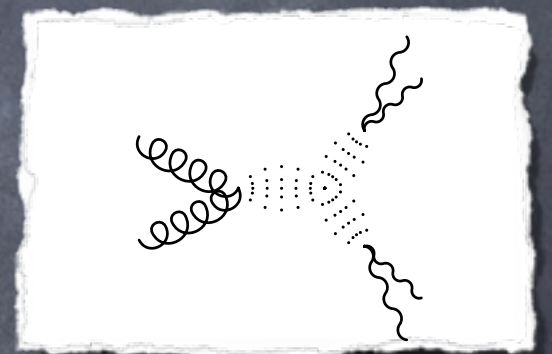
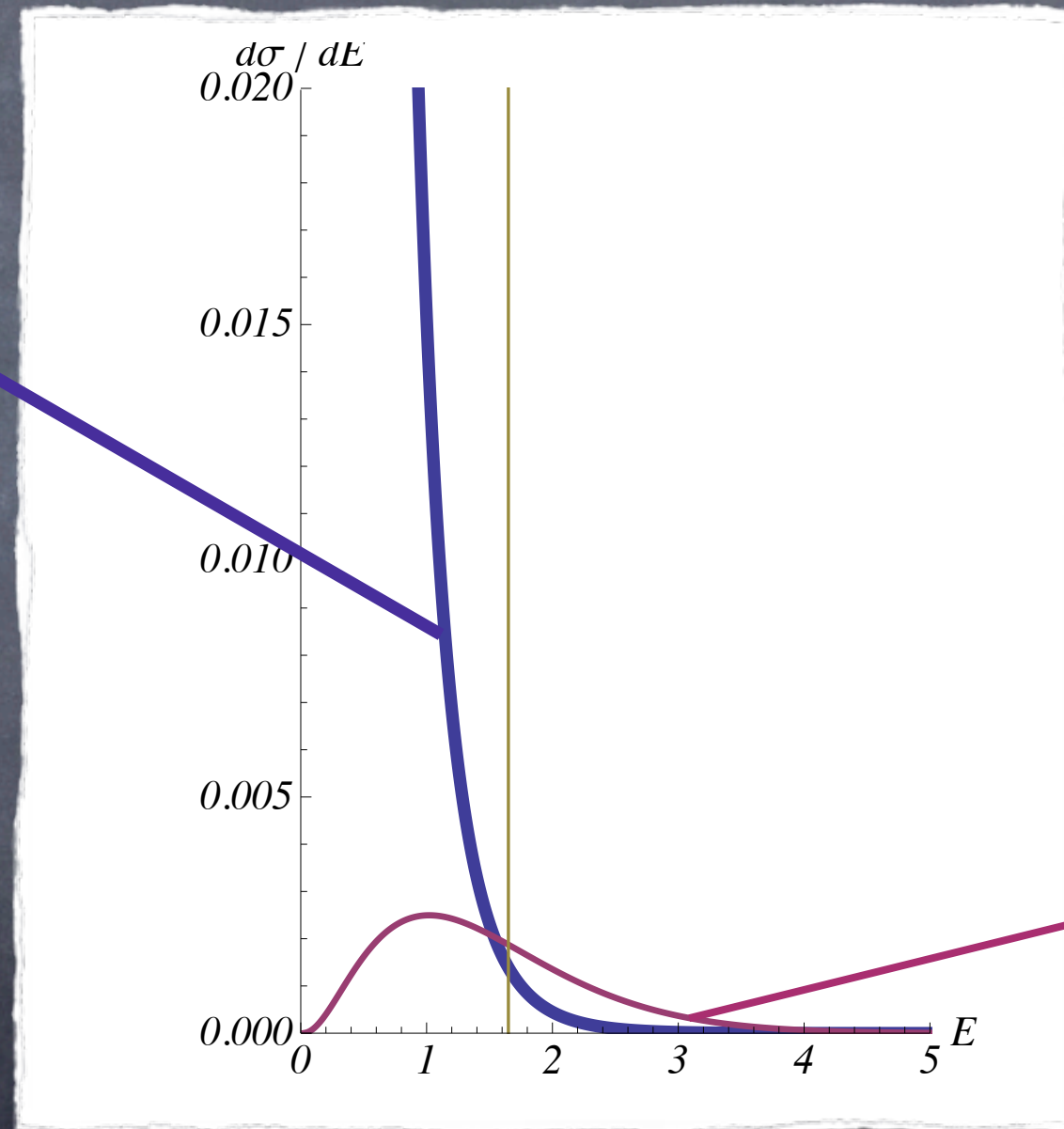
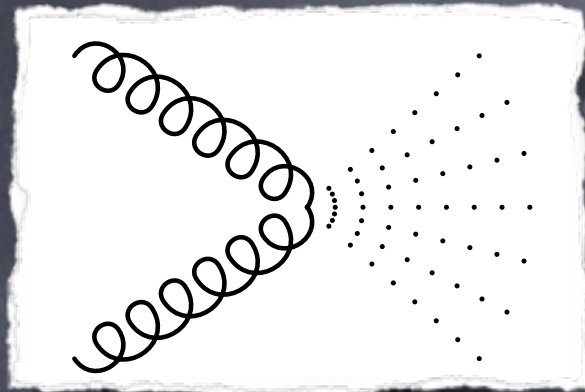
No bound on C_3 available



A. Delgado, M. Strassler
(2009)

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Unitarity bound



A. Delgado, M. Strassler
(2009)

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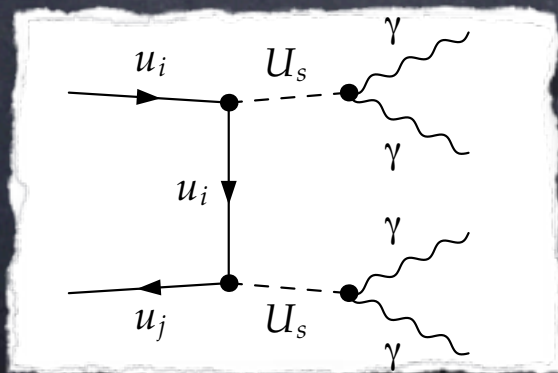
Bound on $\sigma_{gg \rightarrow 4\gamma}$ for 14 TeV LHC

$\Delta_g \setminus \Delta_\gamma$	1.05	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9	2.0
1.05	2.7×10^{-6}	2.7×10^{-5}	4.8×10^{-4}	0.010	0.093	0.62	1.1	1.7	<i>3.8</i>	<i>2.3</i>	<i>1.4</i>
1.1	5.1×10^{-6}	5.2×10^{-5}	6.7×10^{-4}	0.014	0.13	0.89	1.4	1.6	<i>9.6</i>	<i>5.9</i>	<i>3.7</i>
1.2	1.5×10^{-5}	1.4×10^{-4}	1.3×10^{-3}	0.023	0.37	2.4	2.3	1.7	<i>2.3</i>	<i>1.4</i>	<i>7.1</i>
1.3	3.7×10^{-5}	2.8×10^{-4}	3.2×10^{-3}	0.031	0.33	1.7	1.2	0.91	<i>16.</i>	<i>9.3</i>	<i>5.4</i>
1.4	3.3×10^{-5}	2.5×10^{-4}	2.3×10^{-3}	0.023	0.24	1.2	0.73	0.56	<i>12.</i>	<i>7.1</i>	<i>4.5</i>
1.5	3.6×10^{-5}	2.4×10^{-4}	2.8×10^{-3}	0.025	0.19	0.78	0.57	0.37	<i>9.3</i>	<i>5.4</i>	<i>3.2</i>
1.6	3.6×10^{-5}	2.6×10^{-4}	2.3×10^{-3}	0.021	0.16	0.55	0.48	0.31	<i>7.1</i>	<i>4.7</i>	<i>2.5</i>
1.7	4.7×10^{-5}	2.9×10^{-4}	2.7×10^{-3}	0.024	0.16	0.50	0.35	0.26	<i>5.4</i>	<i>3.2</i>	<i>2.0</i>
1.8	4.4×10^{-5}	2.2×10^{-4}	1.7×10^{-3}	0.022	0.20	0.38	0.32	0.23	<i>4.2</i>	<i>2.5</i>	<i>1.5</i>
1.9	3.4×10^{-5}	1.6×10^{-4}	1.5×10^{-3}	0.014	0.15	0.36	0.29	0.23	<i>3.2</i>	<i>2.0</i>	<i>1.2</i>
2.0	2.7×10^{-5}	1.3×10^{-4}	8.7×10^{-4}	0.013	0.14	0.35	0.31	0.24	<i>2.5</i>	<i>1.5</i>	<i>0.96</i>

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Bound on $\sigma_{gg \rightarrow 4\gamma}$ for 14 TeV LHC

$\Delta_g \backslash \Delta_\gamma$	1.05	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9	2.0
1.05	2.7×10^{-6}	2.7×10^{-5}	4.8×10^{-4}	0.010	0.093	0.62	1.1	1.7	<i>3.8</i>	<i>2.3</i>	<i>1.4</i>
1.1	5.1×10^{-6}	5.2×10^{-5}	6.7×10^{-4}	0.014	0.13	0.89	1.4	1.6	<i>9.6</i>	<i>5.9</i>	<i>3.7</i>
1.2	1.5×10^{-5}	1.4×10^{-4}	1.3×10^{-3}	0.023	0.37	2.4	2.3	1.7	<i>2.3</i>	<i>1.4</i>	<i>7.1</i>
1.3	3.7×10^{-5}	2.8×10^{-4}	3.2×10^{-3}	0.031	0.33	1.7	1.2	0.91	<i>16.</i>	<i>9.3</i>	<i>5.4</i>
1.4	3.3×10^{-5}	2.5×10^{-4}	2.3×10^{-3}	0.023	0.24	1.2	0.73	0.56	<i>12.</i>	<i>7.1</i>	<i>4.5</i>
1.5	3.6×10^{-5}	2.4×10^{-4}	2.8×10^{-3}	0.025	0.19	0.78	0.57	0.37	<i>9.3</i>	<i>5.4</i>	<i>3.2</i>
1.6	3.6×10^{-5}	2.6×10^{-4}	2.3×10^{-3}	0.021	0.16	0.55	0.48	0.31	<i>7.1</i>	<i>4.7</i>	<i>2.5</i>
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1.9	3.4×10^{-5}	1.6×10^{-4}	1.5×10^{-3}	0.014	0.15	0.36	0.29	0.23	<i>3.2</i>	<i>2.0</i>	<i>1.2</i>
2.0	2.7×10^{-5}	1.3×10^{-4}	8.7×10^{-4}	0.013	0.14	0.35	0.31	0.24	<i>2.5</i>	<i>1.5</i>	<i>0.96</i>



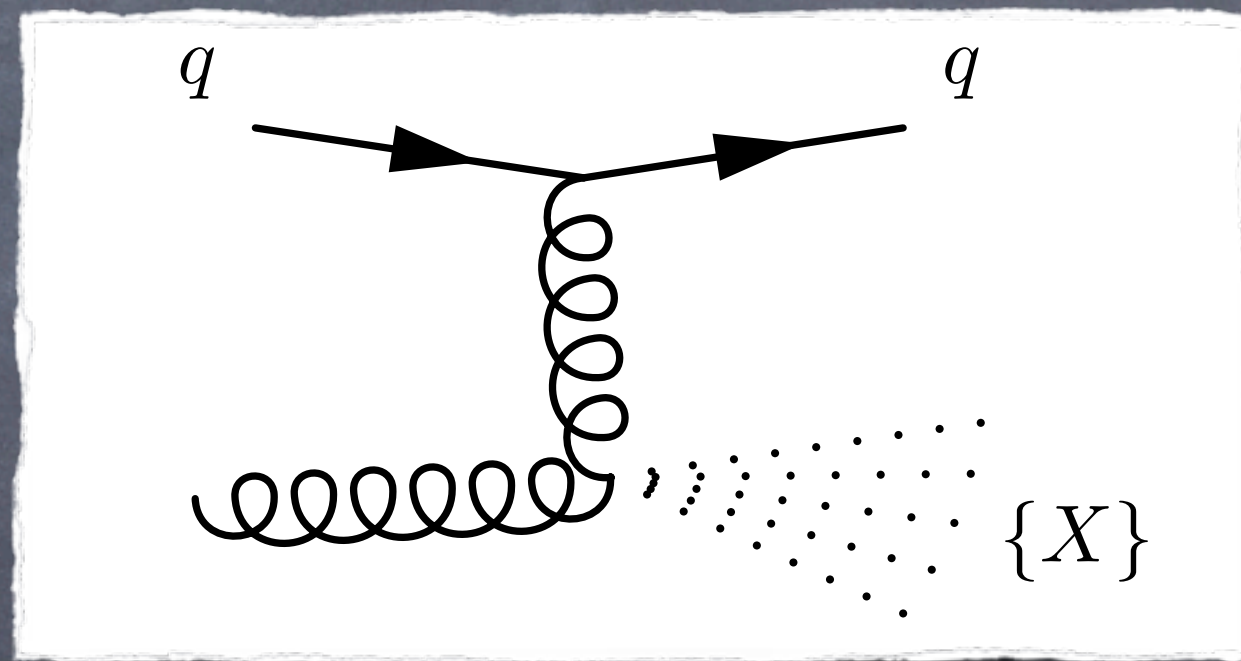
Not accounted for here

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T. Aliev, M. Frank, I. Turan (2009)

Outlook

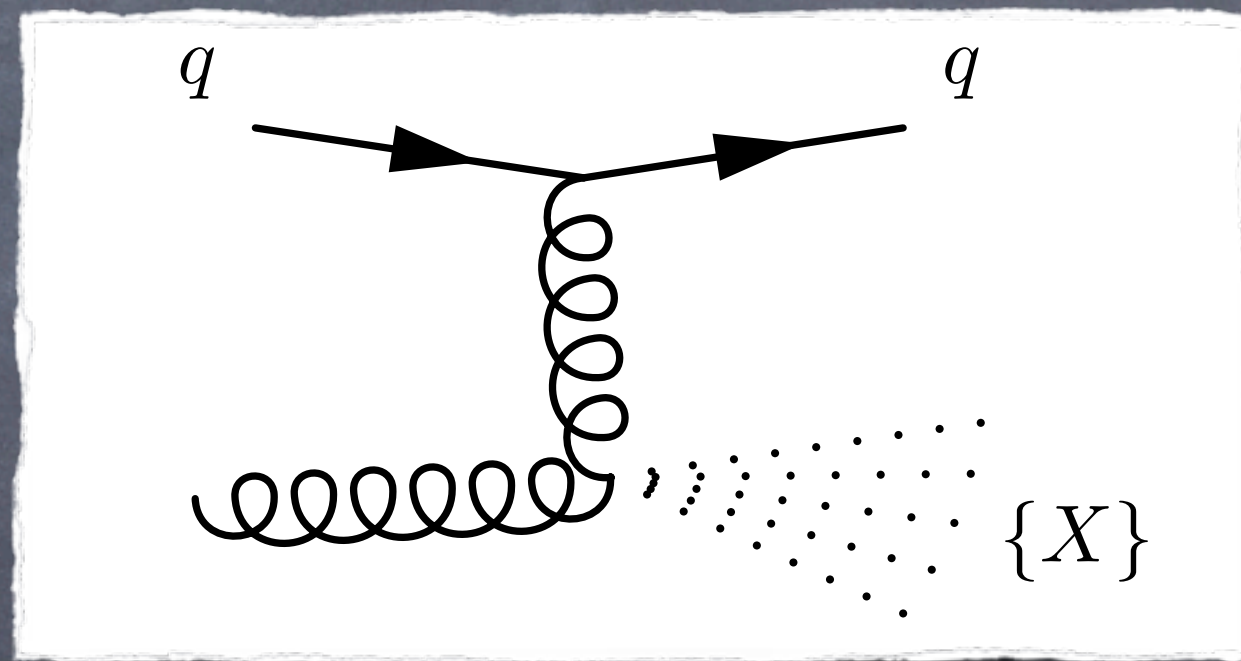
Discovery through Unparticle production
(Jet + MET)



Simon Knapen, Rutgers University

Outlook

Discovery through Unparticle production
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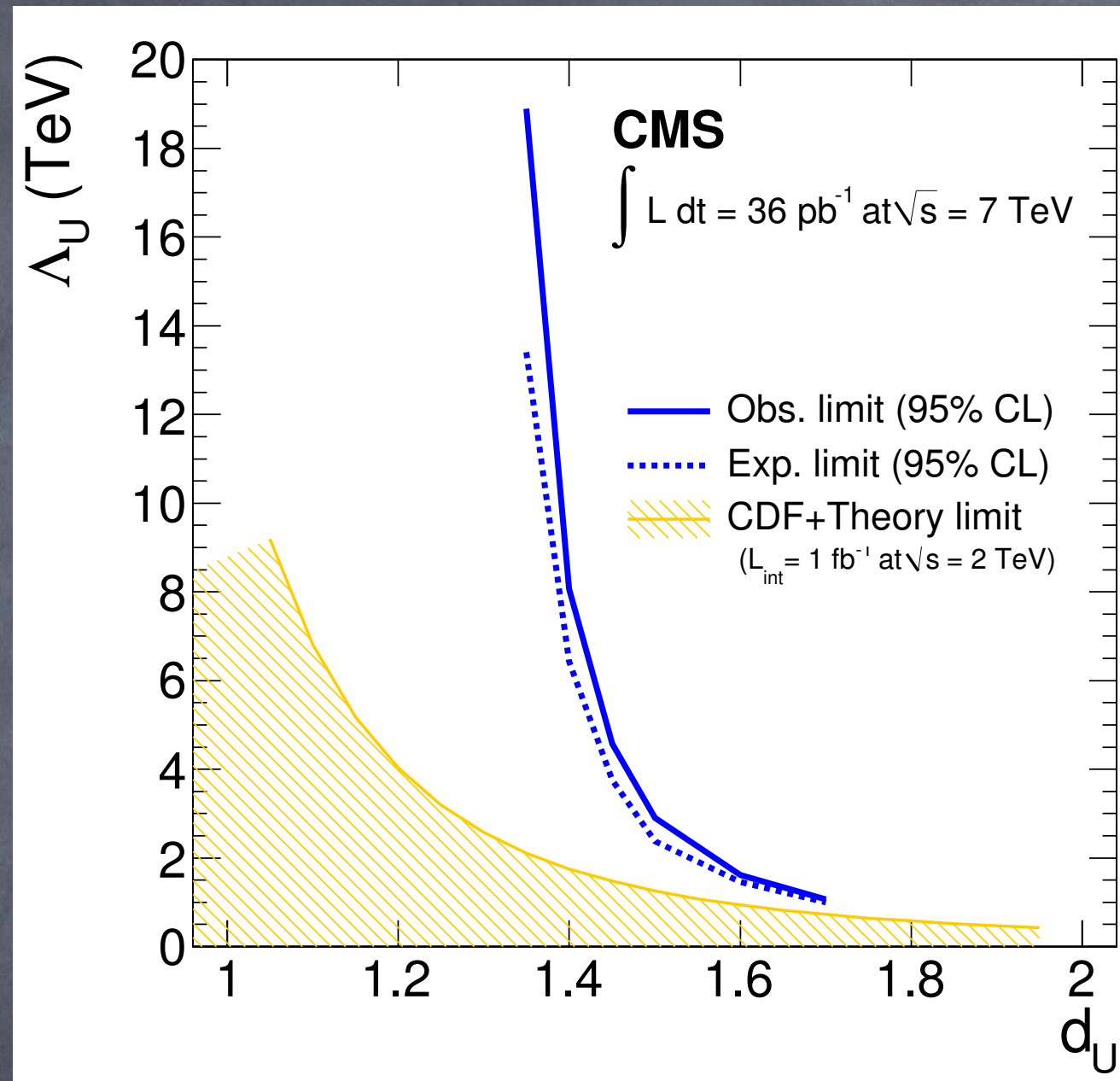


$$\hat{\sigma} \sim \frac{1}{\hat{s}} \left(\frac{\hat{s}}{\Lambda^2} \right)^\Delta$$



Bounds improve rapidly
with increasing \hat{s}

Simon Knapen, Rutgers University



CMS collaboration, June 2011

Simon Knapen, Rutgers University

Conclusions

- Bounds on unparticle interactions with electro-weak gauge bosons range from $\Lambda \sim 200 \text{ GeV} - 50 \text{ TeV}$
- Four photon production through 3-points function can not be discovery channel
- Our bounds will improve dramatically with LHC data

Simon Knapen, Rutgers University

SM couplings

$$\begin{aligned} & \frac{1}{\Lambda^{\Delta-2}} H H^\dagger \mathcal{O}_u, \quad \frac{1}{\Lambda^{\Delta-1}} \bar{f} H f' \mathcal{O}_u, \quad \frac{1}{\Lambda^{\Delta-1}} \bar{f} H \gamma_5 f' \mathcal{O}_u, \quad \frac{1}{\Lambda^\Delta} G_{\alpha\beta} G^{\alpha\beta} \mathcal{O}_u, \\ & \frac{1}{\Lambda^{\Delta-1}} \bar{f} \gamma_\mu f \mathcal{O}_u^\mu, \quad \frac{1}{\Lambda^{\Delta-1}} \bar{f} \gamma_\mu \gamma_5 f \mathcal{O}_u^\mu, \\ & - \frac{1}{4} \frac{1}{\Lambda^\Delta} \bar{f} \left(\gamma_\mu \overleftrightarrow{D}_\nu + \gamma_\nu \overleftrightarrow{D}_\mu \right) f \mathcal{O}_u^{\mu\nu}, \quad \frac{1}{\Lambda^\Delta} G_{\mu\alpha} G_\nu{}^\alpha \mathcal{O}_u^{\mu\nu} \end{aligned}$$

(Unitarity)

$$\Delta_{\mathcal{O}_u} \geq 1$$

$$\Delta_{\mathcal{O}_u^\mu} \geq 3$$

$$\Delta_{\mathcal{O}_u^{\mu\nu}} \geq 4$$

G. Mack (1977)

B. Grinstein, K. Intriligator, I Rothstein (2008)

Simon Knapen, Rutgers University

SM couplings

$$\begin{aligned}
 & \frac{1}{\Lambda^{\Delta-2}} H H^\dagger \mathcal{O}_u, & \frac{1}{\Lambda^{\Delta-1}} \bar{f} H f' \mathcal{O}_u, & \frac{1}{\Lambda^{\Delta-1}} \bar{f} H \gamma_5 f' \mathcal{O}_u, & \frac{1}{\Lambda^\Delta} G_{\alpha\beta} G^{\alpha\beta} \mathcal{O}_u, \\
 & \frac{1}{\Lambda^{\Delta-1}} \bar{f} \gamma_\mu f \mathcal{O}_u^\mu, & \frac{1}{\Lambda^{\Delta-1}} \bar{f} \gamma_\mu \gamma_5 f \mathcal{O}_u^\mu, & & \\
 & -\frac{1}{4} \frac{1}{\Lambda^\Delta} \bar{f} \left(\gamma_\mu \overleftrightarrow{D}_\nu + \gamma_\nu \overleftrightarrow{D}_\mu \right) f \mathcal{O}_u^{\mu\nu}, & \frac{1}{\Lambda^\Delta} G_{\mu\alpha} G_\nu{}^\alpha \mathcal{O}_u^{\mu\nu} & &
 \end{aligned}$$

(Unitarity)

$$\Delta_{\mathcal{O}_u} \geq 1$$

$$\Delta_{\mathcal{O}_u^\mu} \geq 3$$

$$\Delta_{\mathcal{O}_u^{\mu\nu}} \geq 4$$

$$\partial A \partial A \mathcal{O}_u$$

$$\partial A \partial Z \mathcal{O}_u$$

$$\partial G \partial G \mathcal{O}_u$$

} S. Kathrein, SK, M. Strassler
(2010)

A. Delgado, M. Strassler
(2010)

G. Mack (1977)

B. Grinstein, K. Intriligator, I Rothstein (2008)

Simon Knapen, Rutgers University

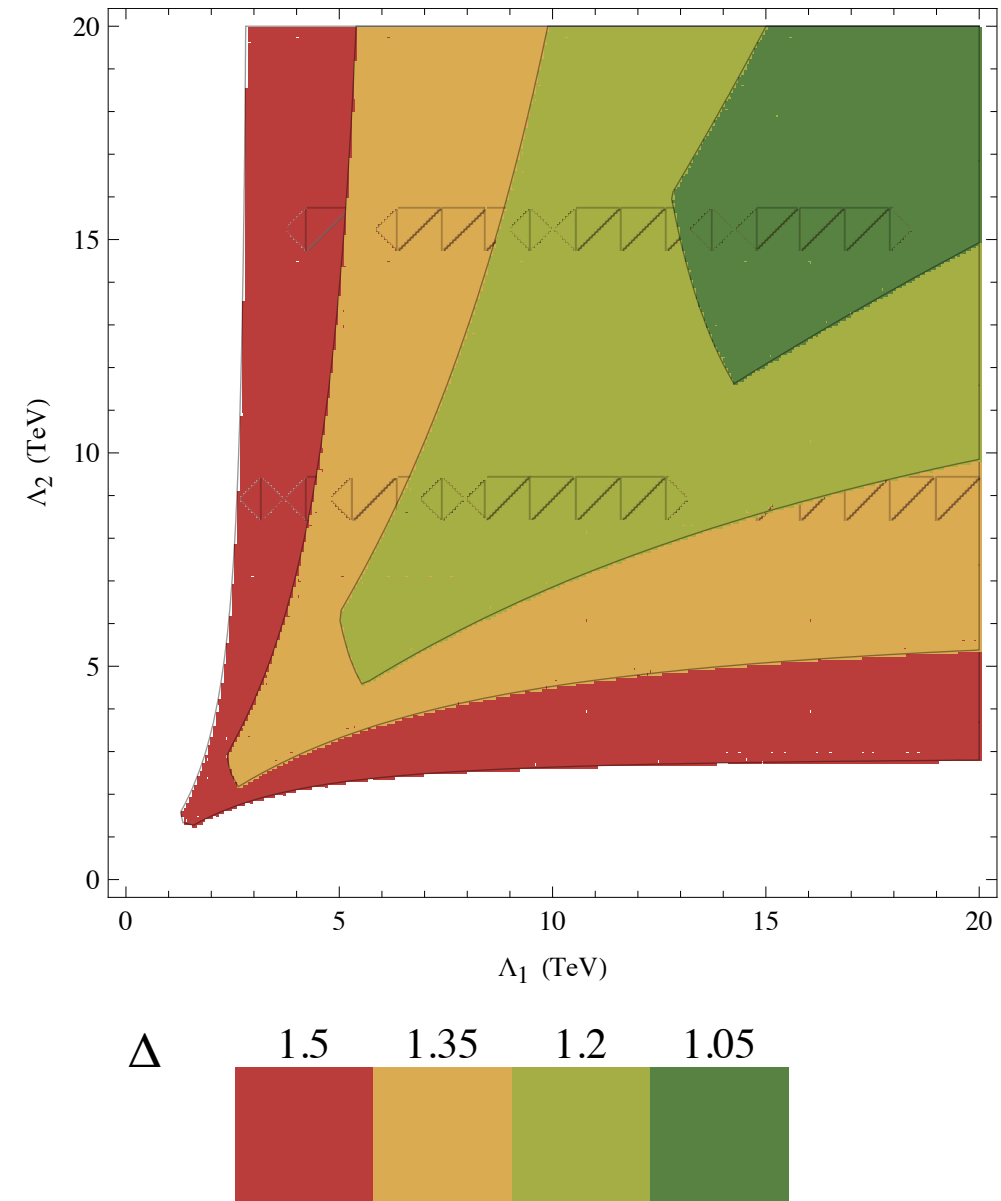
Coupling with W's

$$\frac{\lambda_1}{\Lambda_1^\Delta} B_{\alpha\beta} B^{\alpha\beta} \mathcal{O}_u + \frac{\lambda_2}{\Lambda_2^\Delta} W_{\alpha\beta}^3 W^{3\alpha\beta} \mathcal{O}_u$$



$$\frac{\lambda_{\gamma Z}}{\Lambda_{\gamma Z}^\Delta} \equiv \frac{\lambda_2}{\Lambda_2^\Delta} - \frac{\lambda_1}{\Lambda_1^\Delta}$$

$$\frac{\lambda_\gamma}{\Lambda_\gamma^\Delta} \equiv c_\theta^2 \frac{\lambda_1}{\Lambda_1^\Delta} + s_\theta^2 \frac{\lambda_2}{\Lambda_2^\Delta}$$



Simon Knapen, Rutgers University